## Ordinary exercises:

1. Let $A=\{a, b, c\}, B=\{b, d\}$ ja $C=\{a, c, d, e\}$. Write the following sets explicitly:
a) $A \cup(C-B)$
b) $B \times(A \cap C)$
c) $2^{\{\emptyset\}}-2^{\emptyset}$
2. Let $A=\{a, b, c, d\}$ and a relation $R \subseteq A \times A$ :

$$
R=\{(a, a),(a, b),(a, d),(b, d),(b, c),(c, b),(d, d)\}
$$

Draw directed graphs representing the following relations:
a) $R$
b) $R^{-1}$
c) $\quad R \circ R$
d) $R \cup(R \circ R)$
3. Let $A=\{a, b, c, d\}$ and $R \subseteq A \times A$ :

$$
R=\{(a, b),(b, c),(c, a),(c, c),(d, c)\}
$$

Draw directed graphs representing
a) the transitive closure of $R$;
b) the symmetric closure of $R$; and
c) the reflexive transitive closure of $R$.

## Demonstration exercises:

4. Let $f: A \rightarrow B$. Show that the following relation $R$ is an equivalence relation on $A:(a, b) \in R$ if and only if $f(a)=f(b)$.
5. Prove that if $S$ is any collection of sets, then $R_{s}=\{(A, B) \mid A, B \in$ $S$ and $A \subseteq B\}$ is a partial order.
6. Is the transitive closure of a symmetric closure of a binary relation necessarily reflexive? Prove it or give a counterexample.
7. Let $S$ be any set, and let $\mathcal{P}$ be the set of all partitions of $S$. Let $R$ be the binary relation on $\mathcal{P}$ such that $\left(\Pi_{1} \cdot \Pi_{2}\right) \in R$ if and only if for every $S_{1} \in \Pi_{1}$, there is an $S_{2} \in \Pi_{2}$ such that $S_{1} \subseteq S_{2}$. Show that $R$ is a partial order on $\mathcal{P}$. What elements of $\mathcal{P}$ are minimal and maximal?
