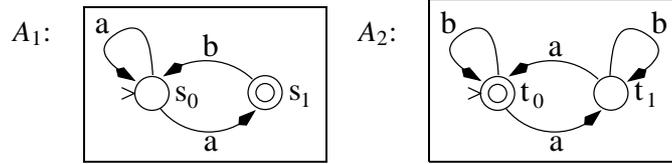
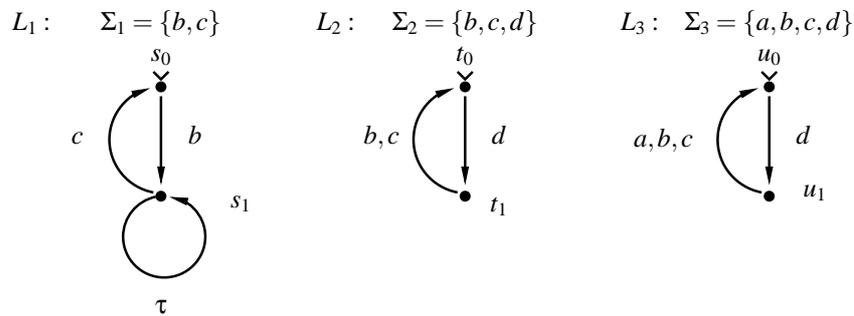


**Assignment 1** Consider the following finite state automata  $A_1$  and  $A_2$ , where  $\Sigma_1 = \Sigma_2 = \{a, b\}$ .



- Construct the finite state automaton  $A_a = A_1 \cap A_2$ .
- Construct the finite state automaton  $A_b$  that accepts the complement of the language accepted by the automaton  $A_a$ .

**Assignment 2** Consider the following three labelled transition systems (LTSs)  $L_1$ ,  $L_2$ , and  $L_3$ :



- Compute the parallel composition  $L = L_1 || L_2 || L_3$ .
- Does  $L$  contain any conflicts? If it does, please give a list consisting of all the triples  $(v, t, t')$ , where:  $v$  is a global state of  $L$  where a conflict occurs and  $t, t'$  are a pair of global transitions of  $L$  which are in conflict in  $v$ .
- Does  $L$  contain any deadlocks? If it does, please give a list of global states of  $L$  which are deadlocks.
- Does  $L$  contain any livelocks? If it does, please give a list of global states of  $L$  in which a livelock exists.
- Does  $L$  contain a pair of independent transitions? If it does, give one example of two global transitions which are independent.
- Give a deterministic finite automaton  $A_f$  accepting the language  $\Sigma^* \setminus \text{traces}(L)$ , where  $\Sigma$  is the alphabet of  $L$ .
- Answer the question: Is  $\text{traces}(L_3) \subseteq \text{traces}(L)$ ? Please use the automaton  $A_f$  constructed in the previous step. If the answer is no, give a word in  $\text{traces}(L_3) \setminus \text{traces}(L)$ .

**Note! More assignments on the other side of the paper.**

- Assignment 3**
- (a) Let  $L$  be a parallel composition of LTSs  $L = L_1 || L_2 || \dots || L_n$  with  $n$  global transitions enabled in the initial state that are all pairwise independent, and in which each transition becomes disabled after its firing. How many states does the reachability graph of  $L$  at least have? How many edges does the reachability graph of  $L$  at least have? (In both cases give as tight a lower bound as possible as a function of the parameter  $n$ .)
- (b) Give two LTSs  $L_b$  and  $L'_b$  such that  $L_b \leq_{tr} L'_b$  holds but  $L'_b \leq_{tr} L_b$  does not hold.
- (c) Give two LTSs  $L_c$  and  $L'_c$  such that  $L_c \leq_{sim} L'_c$  holds but  $L'_c \sim L_c$  does not hold.
- (d) Is the following claim true: If both  $L_d \leq_{sim} L'_d$  and  $L'_d \leq_{sim} L_d$  hold, then  $L_d$  and  $L'_d$  are bisimilar. Please explain your answer in a sentence or two.
- (e) Define formally the notion: Bisimulation.

**Assignment 4** Give the formalisation of the following properties as past safety formulas:

- (a) Processes 0 and 1 are never at the same time in the critical section. Use atomic propositions:  $cs_0$  - process 0 is in the critical section, and  $cs_1$  - process 1 is in the critical section.
- (b) If a lock is released, it has been locked in the past. Use atomic propositions:  $release$  - the lock is being released, and  $lock$  - the lock is being locked.
- (c) If the alarm is on, the system has crashed in the past and has not been reset after crashing. Use atomic propositions:  $alarm$  - the alarm is on,  $crashed$  - the system crashed, and  $reset$  - the system is being reset.

**Assignment 5** Create the reachability graph  $G$  of the P/T-net  $N$  below.

