[Only two problems this time.]

1. Consider the following $k$-Set Splitting problem: Given a collection $C$ of $k$-element subsets of a finite set $S$, is there a subset $S' \subseteq S$ such that no $C \in C$ is contained in either $S'$ or $S - S'$ (i.e., $S'$ “splits” all the sets in $C$ in two pieces). The problem is NP-complete for $k \geq 3$. Make an educated guess concerning the location of “hard instances” for this problem.

2. Consider the problem for which you programmed a local search method in your first programming assignment. Can you identify a parameter $\beta$ in the problem analogous to the clauses-to-variables ratio $\alpha$ of the Satisfiability problem? At which values of $\beta$ would you guess that your problem would be most difficult to solve? [Highly optional: Make some relevant computer experiments using your existing local-search code, e.g.: (a) plot the time evolution of the problem’s objective function for different types of input instances (if there is a lot of variance in the time series, take averages over several runs with different random number sequences); (b) try to experimentally determine the region of “hard instances” for the problem.]