Tutorial problems

- **1.** (a) Write down a program P such that $\models_p [true] P [y==x+2]$ holds and prove that this is so.
 - (b) Write down a program P such that P contains an if-statement and

$$\models_p [\text{true}] P [z > x + y + 4]$$

holds, and prove that this is so.

2. Show that the following holds for program Prog:

$$\models_p [\text{true}] \text{Prog} [x == v - z],$$

where Prog is as follows:

```
x = 0;
y = 0;
while(!(y == z)) {
    y = y + 1;
    x = x - 1
}
x = x + v;
```

- **3.** (a) For any B_1 , B_2 and P explain why $\models_p [B_1] P [B_2]$, whenever the relation $\models_t [B_1] P [B_2]$ holds.
 - (b) Show that the following holds for program Prog in Exercise 2:

$$\models_t [z \ge 0] Prog [x == v - z].$$

Demonstration problems

4. Use propositional logic to prove the equivalence of the following statements.

(a)
$$!(a==b||a$$

```
(b) a!=b\&\&!(b>a)
```

5. Prove the partial correctness in the following cases.

```
(a) \models_p [x>0] y=x+1 [y>1]

(b) \models_p [true] y=x; y=x+x+y [y==3*x]

(c) \models_p [x>1] a=1; y=x; y=y-a [y>0 &&x>y]
```

6. Show that $\models_p [true] P [z == min(x,y)]$, where P is the following program:

```
if(x>y) then {
    z = y
} else {
    z = x
}
```

7. Show that

```
(a) \models_p [true] Sum [z == x + y]

(b) \models_t [0 <= y] Sum [z == x + y]
```

where Sum is the following program:

```
z = x;
v = y;
while(!(v == 0)) {
    z = z + 1;
    v = v - 1
}
```