## **Some Incomplete Constraint Solvers**

Pages: 178 – 196 Andreas Anderson Andreas.Anderson@hut.fi 2004/02/26

1.

a) Equality and Disequality Constraints

Apply the rules of *EQU* proof system to the following CSP as many times as possible:

$$\langle x_1 \neq x_3, x_1 = x_6, x_4 = x_4, x_3 \neq x_6, x_5 \neq x_4, x_5 \neq x_7; x_1 \in \{a, b, c, d\}, x_2 = n,$$
  
 $x_3 = d, x_4 \in \{e, r\}, x_5 = e, x_6 \in \{a, r, s\}, x_7 \in \{e, s\} \rangle$ 

b) Inequality Constraints on Integer Intervals

Apply LINEREAR INEQUALITY 1 rule once to the following CSP:

$$\langle x_1 + 2x_2 - 3x_3 \le 4; x_1 \in [1..10], x_2 \in [2..20], x_3 \in [-10..10] \rangle$$

2.

a) Boolean Constraints

Transform the following Boolean constraints to *simple* form:

(i) 
$$x_1 \wedge (x_2 \vee x_3) = x_4$$

$$(ii) \qquad \neg (x_1 \land (x_2 \land x_3)) = x_4$$

(iii) 
$$(x_1 \lor (x_2 \land x_3)) \lor x_4 = x_5$$

b) Boolean Constraints

Apply at least two rules from the proof system *BOOL* to the following CSP:

$$\langle (x_1 \land x_2) \lor (x_2 \land x_3) = x_4, \neg x_1 \land (x_5 \lor x_6) = x_7 \land (x_2 \land x_3);$$
  
 $x_1 \in \{0,1\}, x_2 = 1, x_3 = 1, x_4 \in \{0,1\}, x_5 = 1, x_6 \in \{0,1\}, x_7 = 1 \rangle$