

**T-79.186**  
**Reactive Systems**  
**Home Exercise 3**  
**Deadline 3.3 16.15**

**Spring 2004**

Return your answers by email (Postscript or PDF) to Timo.Latvala@hut.fi, or on paper to the lecture. Remember to include your name *and* student number.

For this home exercise round use the automata definition used in the lecture slides.

- 1.)
  - (a) Given atomic propositions  $TRY0$  and  $CR0$ , create an automaton  $S_1$ , which accepts all (finite) sequences of valuations such that if  $CR0$  holds at some index, then  $TRY0$  has held at some earlier index.
  - (b) Given the atomic propositions  $P, Q$  and  $R$ , create an automaton  $S_2$ , which accepts all (finite) sequences of valuations such that  $P$  precedes  $Q$  before  $R$ . Tip:  $R$  and  $Q$  do not have to become true at any point.
- 2) Express the following properties in LTL. (First define the atomic propositions and their meaning.)
  - (a) If message “m1” is sent infinitely many times by the sender, then the message “m1” is received infinitely often by the receiver.
  - (b) Only finitely many messages are lost by the data channel “d1”.
  - (c) Always when process “p1” is in the critical section, it will go to non-critical in a finite amount of time steps.
  - (d) If a message “m2” is received by the receiver, then the message “m2” was sent before (or at the same time moment) by the sender.
  - (e) If an addition is fed to a pipelined ALU unit, then the result is ready four time units later (use the  $X$ -operator to denote one time unit).
- 3) For each item below, give a Kripke structure which satisfies (in the initial state) the  $CTL^*$  formula (check the semantics from Berard et al, page 34) in question. Remember that in a Kripke structure each state has at least one successor.
  - (a)  $EF(p \wedge (EFq \wedge AX\neg q))$
  - (b)  $((EXEG(p)) \wedge (EX(AF\neg p)))$
  - (c)  $\neg AGF(p)$
  - (d)  $A(GF(p) \Rightarrow GF(q))$