

T-79.159

Cryptography and Data Security

Lecture 5:

4.1 MAC-functions

4.2 Hash-functions

Kaufman et al: Ch 5

Stallings: Ch 11, Ch 12

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5.1.Message authentication codes (MAC)

(Secret key , Message) $\rightarrow$ MAC

- A MAC of a message P of arbitrary length is computed as a function $H_K(P)$ of P under the control of a secret key K . The MAC is appended to the message by the sender.
- Given a message P and its MAC value M , the MAC can be verified by anybody in possession of the secret key K and the MAC computation algorithm.
- The MAC length m is fixed.
- Security requirement: it must be infeasible, without the knowledge of the secret key, to determine the correct value of $H_K(P)$ with a success probability larger than $1/2^m$. This is the probability of simply guessing the MAC value correctly at random. It should not be possible to increase this probability even if a large number of correct pairs P and $H_K(P)$ is available to the attacker.

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An Example: A Weak MAC

E_K is an encryption function of a block cipher

Given a message $P = P_1, P_2, \dots, P_n$

a MAC is computed as

$$H_K(P) = E_K(P_1 \oplus P_2 \oplus \dots \oplus P_n)$$

Then it is easy to produce a different message P' with an equal MAC:

$$P' = P'_1, P'_2, \dots, P'_{n-1}, \left(\bigoplus_{i=1}^{n-1} P'_i \right) \oplus \left(\bigoplus_{i=1}^n P_i \right)$$

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Derived security requirements

The requirement: It must be infeasible, without the knowledge of the secret key, to determine the correct value of $H_K(P)$ with a success probability larger than $1/2^m$.

This means, in particular, that the following are satisfied

- Given a message P and $M = H_K(P)$ it should be infeasible to produce a modified message P' such that $H_K(P') = M$ without the knowledge of the key
- For each K , the function $P \rightarrow H_K(P)$ is one-way
- Given known MACs for a number of known (or chosen or adaptively chosen) messages, it should be infeasible to derive the key.

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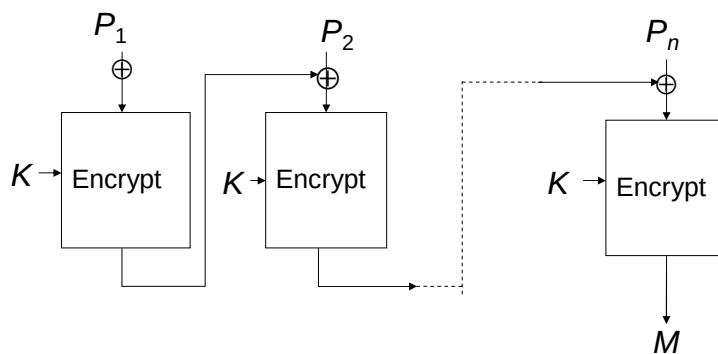
MAC Designs

- Similarly as block ciphers, MAC algorithms operate on relatively large blocks of data.
- Most MACs are iterated constructions. The core function of the MAC algorithm is a compression function. At each round the compression function takes a new data block and compresses it together with the compression result from the previous rounds. Hence the length of the message to be authenticated determines how many iteration rounds are required to compute the MAC value.

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CBC MAC

A MAC mode of operation of any block cipher

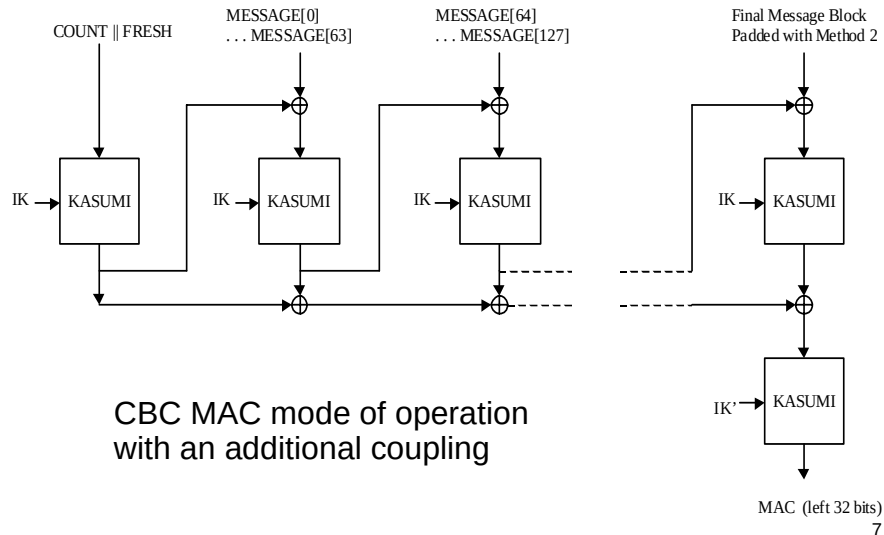


- CBC encryption with fixed IV = 00...0. The last ciphertext block (possibly truncated) is taken as the MAC.

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Integrity function f9



CRC MAC

- A MAC for stream ciphers (see HAC 9.5.4.)
- Idea: A simple (cryptographically unsecure) error detecting check sum is encrypted using non-repeating keystream (ideally, a one-time pad)

An n -bit message $P = p_0, p_1, \dots, p_{n-1}$ is associated with the polynomial

$$P(x) = p_0 + p_1x + p_2x^2 + \dots + p_{n-1}x^{n-1}$$

The secret key K consists of a polynomial $q(x)$ of degree m , and an m -bit one-time key stream string $(k_0, k_1, k_2, \dots, k_{m-1})$.

First the remainder $c_0 + c_1x + c_2x^2 + \dots + c_{m-1}x^{m-1}$ of the polynomial division $P(x)/q(x)$ is computed. The MAC is computed as the xor of the key stream string and the remainder string $(c_0, c_1, c_2, \dots, c_{m-1})$ as

$$(c_0 \oplus k_0, c_1 \oplus k_1, c_2 \oplus k_2, \dots, c_{m-1} \oplus k_{m-1})$$

Note: The polynomial $q(x)$ can be reused for different messages

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Polynomial MAC

- Another MAC for stream ciphers
- Idea: An (cryptographically unsecure) error detecting code is encrypted using non-repeating keystream (ideally, a one-time pad)

An n -block message $P = P_0, P_1, \dots, P_{n-1}$ with block size m bits is associated with the polynomial with m -bit coefficients:

$$P(x) = P_0 + P_1x + P_2x^2 + \dots + P_{n-1}x^{n-1}$$

Also the value of the polynomial is assumed to be expressed as an m -bit string.

The secret key K consists of a point $x = X$ and an m -bit one-time key stream string $(k_0, k_1, k_2, \dots, k_{n-1})$.

First the message polynomial is evaluated at the point X . Let us denote the value by $(c_0, c_1, c_2, \dots, c_{m-1})$. The MAC is computed as the xor of the key stream string and the value as

$$(c_0 \oplus k_0, c_1 \oplus k_1, c_2 \oplus k_2, \dots, c_{m-1} \oplus k_{m-1})$$

Note: The point X can be reused for different messages

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An Example

Poly1305-AES MAC

- By D J Bernstein, presented at FSE2005, <http://cr.yp.to/mac.html>
- Over finite fields: Carter-Wegman MAC and Galois MAC (with Counter Mode key stream generator)

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Combined modes of operation

- CCM: Counter mode encryption and CBC MAC , see:
 - 1) IETF RFC 3610
 - 2) NIST Special Publication SP800-38C (with consideration to the IEEE 802.11i)(see Exercise 3.5)
- GCM: Counter mode encryption and a Polynomial-based MAC over Galois Field, see:
<http://csrc.nist.gov/CryptoToolkit/modes/proposedmodes/>

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Hash functions

Message $\rightarrow$ Hash code

- A hash code of a message P of arbitrary length is computed as a function $H(P)$ of P . The hash length m is fixed.
- Hash function is public: Given a message P anybody can compute the hash code of P .
- Security requirements:
 1. *Preimage resistance*: Given h it is impossible to find P such that $H(P) = h$
 2. *Second preimage resistance*: Given P it is impossible to find P' such that $H(P') = H(P)$
 3. *Collision resistance*: It is impossible to find P and P' such that $P \neq P'$ and $H(P') = H(P)$

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Design Principles

- Similarly as MAC algorithms, hash functions operate on relatively large blocks of data.
- Most hash functions are iterated constructions. The core function in a hash function is a compression function. At each round the compression function takes a new data block and compresses it together with the compression result from the previous rounds. Hence the length of the message to be authenticated determines how many iteration rounds are required to compute the MAC value.

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SHA-1

- Designed by NSA
- FIPS 180-1 Standardi 1995 –
www.itl.nist.gov/fipspubs/fip180-1.htm

February 2005:

Professor Xiaoyun Wang (Shandong University)
announce an algorithm which finds collisions for SHA-1
with complexity 2^{69}

Recommendation: Use 256- or 512-bit versions of SHA:
csrc.nist.gov/publications/fips/fips180-2/fips180-2.pdf

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SHA-1

- Step 1: Padding
- Step 2: Append length before padding (64 bits); $\text{length} + 64 < 512 L$
- Step 3: Initialise MD buffer CV_0 with five 32-bit registers (A,B,C,D,E)
- Step 4 (repeated L times): Process message in 512-bit (16-word) blocks. It takes 80 rounds. At the end, the contents of the registers ABCDE are added to the input CV_q . The addition modulo 2^{32} is done for each word separately. The result is the output CV_{q+1} (input to the next round), $q = 0, 1, \dots, L-1$. The addition modulo 2^{32} is done for each word separately.
- Step 5: Output is CV_L

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[illegible]

Function F and data expansion

$$q = 0, \dots, 19: F_q(B, C, D) = (B \wedge C) \vee (\bar{B} \wedge D)$$

$$q = 20, \dots, 39: F_q(B, C, D) = B \oplus C \oplus D$$

$$q = 40, \dots, 59: F_q(B, C, D) = (B \wedge C) \vee (B \wedge D) \vee (C \wedge D)$$

$$q = 60, \dots, 79: F_q(B, C, D) = B \oplus C \oplus D$$

Data expansion:

$(W_0, W_1, W_2, \dots, W_{15})$ = the 512-bit input data block

$$W_q = \lll_1 (W_{q-16} \oplus W_{q-14} \oplus W_{q-8} \oplus W_{q-3}), q = 16 \dots 79$$

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Revised SHA Standard

csrc.nist.gov/publications/fips/fips180-2/fips180-2.pdf

	SHA-1	SHA-256	SHA-384	SHA-512
Hash size	160	256	384	512
Message size	$< 2^{64}$	$< 2^{64}$	$< 2^{128}$	$< 2^{128}$
Block size	512	512	1024	1024
Word size	32	32	64	64
Number of steps	80	80	80	80
Claimed security	80	128	192	256

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