### T-79.159 Cryptography and Data Security Lecture 3: 3.1 Introduction to block ciphers

3.1 Introduction to block ciphers 3.2 DES 3.3 IDEA 3.4 AES Kaufman et al: Chapter 3 Stallings: Chapters 3, 5



#### Block ciphers, design principles

- The ultimate design goal of a block cipher is to use the secret key as efficiently as possible.
- Confusion and diffusion (Shannon)
- New design criteria are being discovered as response to new attacks.
- A state-of-the-art block cipher is constructed taking into account all known attacks and design principles.
- But no such block cipher can become provably secure, it may remain open to some new, unforeseen attacks.

3

- Common constructions with iterated round function
  - Substitution permutation network (SPN)
  - Feistel network

DES Data Encryption Standard 1977 - 2002 Standard for 25 years Finally found to be too small. DES key is only 56 bits, that is, there are about 10<sup>16</sup> different keys. By manufacturing one million chips, such that, each chip can test one million keys in a second, then one can find the key in about one minute. The EFF DES Cracker built in 1998 can search for a key in about 4,5 days. The cost of the machine is \$250 000. DES has greately contributed to the development of cryptologic research on block ciphers. The design was a joint effort by CIA and IBM. The design principles were not published until little-by-little. The complete set of design criteria is still unknown. Differential cryptanalysis 1989 Linear cryptanalysis 1993 4

















#### The Security of IDEA

- IDEA has been around almost 15 years
- Designed by Xuejia Lai and Jim Massey
- Its only problem so far is its small block size
- Numerous analysis has been published, but nothing substantial
- It is not available in public domain, except for research purposes
- It is available under licence
- It is widely used, e.g in PGP (see Lecture 11)

13



## **Rijndael - Internal Structure**

**Rijndael** is an iterated block cipher with variable length block and variable key size. The number of rounds is defined by the table:

|        | Nb = 4 Nb = 6 |    | Nb = 8 |
|--------|---------------|----|--------|
| Nk = 4 | 10            | 12 | 14     |
| Nk = 6 | 12            | 12 | 14     |
| Nk = 8 | 14            | 14 | 14     |
|        |               |    |        |
| L      | 4 5 0         |    |        |

| AES |  |
|-----|--|
|-----|--|

Nb = length of data block in 32-bit words

Nk = length of key in 32-bit words





















# Mix Column - Design view

The columns of the State are considered as polynomials over  $GF(2^8)$ . They are multiplied by a fixed polynomial c(x) given by

 $c(x) = 03' x^{3} + 01' x^{2} + 01' x + 02'$ 

The product is reduced modulo  $x^4 + 01'$ .

Matrix form

| · -              |   | Г  |    |    | -  | ור               |
|------------------|---|----|----|----|----|------------------|
| b <sub>0,j</sub> |   | 02 | 03 | 01 | 01 | a <sub>0,j</sub> |
| b <sub>1,j</sub> | = | 01 | 02 | 03 | 01 | a <sub>1,j</sub> |
| b <sub>2,j</sub> |   | 01 | 01 | 02 | 03 | a <sub>2,j</sub> |
| b <sub>3,j</sub> |   | 03 | 01 | 01 | 02 | a <sub>3,j</sub> |

The Inverse Mix Column polynomial is  $c(x)^{-1} \mod (x^4 + 01') = d(x)$  given by

 $d(x) = 'OB' x^3 + 'OD' x^2 + 'O9' x + 'OE'$ 

25







#### **AES** encryption

state  $x^{(r)} = (x_{ij}^{(r)}), \quad i, j = 0,1,2,3, \quad r = 1,2,...,10, \quad x_{ij}^{(r)} \in GF(2^8)$ key  $k^{(r)} = (k_{ij}^{(r)}), \quad i, j = 0,1,2,3, \quad r = 0,1,2,...,10, \quad k_{ij}^{(r)} \in GF(2^8)$ AES encryption:  $x^{(1)} = p \oplus k^{(0)}$   $x^{(r+1)} = M(S(F(G(x^{(r)}))) \oplus k^{(r)}, r = 1,2,...,9)$   $c = S(F(G(x^{(10)}))) \oplus k^{(10)}$ where M, S are linear functions over  $GF(2^8)$  G = (g) where  $g: GF(2^8) \to GF(2^8), g(x) = x^{-1}, g(0) = 0$ F = (f) where  $f - \lambda_0$  is additive over  $GF(2^8)$