Helsinki University of Technology Laboratory for Theoretical Computer Science Pekka Orponen

T-79.148 Introduction to Theoretical Computer Science (2 cr) Exam 11 Feb 2002, 4-7 p.m. T1+T2

Write down on each answer sheet:

- Your name, department, and study book number
- The text: "T-79.148 Introduction to Theoretical Computer Science 11.2.2002"
 - 1. Construct deterministic finite automata accepting each of the following languages:
 - (a) $\{w \in \{a,b\}^* \mid w \text{ contains both } aa \text{ and } bb \text{ as substrings}\};$
 - (b) $\{w \in \{a, b\}^* \mid w \text{ does not contain the substring } aba\};$
 - (c) $\{w \in \{a,b\}^* \mid w \text{ contains a number of } a \text{'s that is an exact multiple of three} \}$.
 - 2. Construct in a systematic way a deterministic finite automaton for the language denoted by the regular expression $(ba)^*b \cup (b^*a)$. (Note: Also the intermediate stages of the construction must be presented the final result alone does not suffice.)
 - 3. Construct a context-free grammar that generates the language

$$L = \{a^i b^j c^k \mid i, j, k \ge 0, i + j = k\}.$$

Prove, furthermore, that the language L is not regular.

4. Construct a Turing machine that decides the language

$$\{w \in \{a, b\}^* \mid w \text{ contains equally many } a\text{'s and } b\text{'s}\}.$$

- 5. Define formally the following notions:
 - (a) Turing-decidable and undecidable languages. Give an example of a language that is recursively enumerable, but not Turing-decidable. (A precise definition is required, but no proofs.)
 - (b) Language classes P and NP; NP-complete languages. Give an example of an NP-complete language. (A precise definition is required, but no proofs.)

Each problem 6 points, total 30 points.