Tik-79.146 **Kevät 1998**
Logiikka tietotekniikassa: erityiskysymyksiä I
Laskuharjoitus 8
Ratkaisut

1. a)

1.	$\langle 1\rangle\neg\big(\Box P \to \Box(Q \to P)\big)$	
2.	$\langle 1\rangle\Box P$	(1)
3.	$\langle 1\rangle\neg\Box(Q \to P)$	(1)
4.	$\langle 1,2\rangle\neg(Q \to P)$	(3)
5.	$\langle 1,2\rangle Q$	(4)
6.	$\langle 1,2\rangle\neg P$	(4)
7.	$\langle 1,2\rangle P$	(2)
	$\otimes$	

b)

1.	$\langle 1\rangle\neg\big(\Box(P \to Q) \to (\neg\Box\neg P \to \neg\Box\neg Q)\big)$			
2.	$\langle 1\rangle\Box(P \to Q)$			(1)
3.	$\langle 1\rangle\neg(\neg\Box\neg P \to \neg\Box\neg Q)$			(1)
4.	$\langle 1\rangle\neg\Box\neg P$			(3)
5.	$\langle 1\rangle\neg\neg\Box\neg Q$			(3)
6.	$\langle 1\rangle\Box\neg Q$			(5)
7.	$\langle 1,2\rangle\neg\neg P$			(4)
8.	$\langle 1,2\rangle P$			(7)
9.	$\langle 1,2\rangle\neg Q$			(6)
10.	$\langle 1,2\rangle(P \to Q)$			(2)
11.	$\langle 1,2\rangle\neg P$	(10)	12. $\langle 1,2\rangle Q$	(10)
	$\otimes$		$\otimes$	

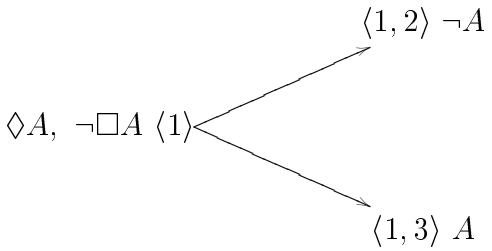
c)

1.	$\langle 1\rangle\neg\big((\Box P \wedge \Box Q) \to \Box(P \wedge Q)\big)$			
2.	$\langle 1\rangle\Box P \wedge \Box Q$			(1)
3.	$\langle 1\rangle\neg\Box(P \wedge Q)$			(1)
4.	$\langle 1\rangle\Box P$			(2)
5.	$\langle 1\rangle\Box Q$			(2)
6.	$\langle 1,2\rangle\neg(P \wedge Q)$			(3)
7.	$\langle 1,2\rangle P$			(4)
8.	$\langle 1,2\rangle Q$			(5)
9.	$\langle 1,2\rangle\neg P$	(6)	10. $\langle 1,2\rangle\neg Q$	(6)
	$\otimes$		$\otimes$	

2. a)

1.	$\langle 1\rangle\neg(\Diamond A \to \Box A)$	
2.	$\langle 1\rangle\Diamond A$	(1)
3.	$\langle 1\rangle\neg\Box A$	(1)
4.	$\langle 1\rangle\neg\Box\neg A$	(2)
5.	$\langle 1,2\rangle\neg A$	(3)
6.	$\langle 1,3\rangle\neg\neg A$	(4)
7.	$\langle 1,3\rangle A$	(6)

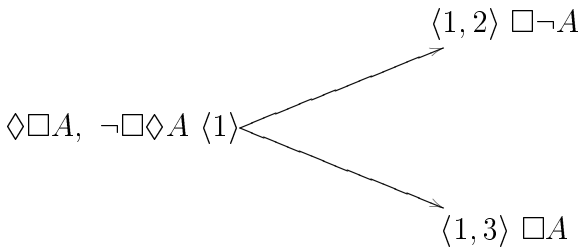
Ei **K**-pätevä.



b)

1.	$\langle 1\rangle\neg(\Diamond\Box A \to \Box\Diamond A)$	
2.	$\langle 1\rangle\Diamond\Box A$	(1)
3.	$\langle 1\rangle\neg\Box\Diamond A$	(1)
4.	$\langle 1\rangle\neg\Box\neg\Box A$	(2)
5.	$\langle 1,2\rangle\neg\Diamond A$	(3)
6.	$\langle 1,3\rangle\neg\neg\Box A$	(4)
7.	$\langle 1,2\rangle\neg\neg\Box\neg A$	(5)
8.	$\langle 1,3\rangle\Box A$	(6)
9.	$\langle 1,2\rangle\Box\neg A$	(7)

Ei **K**-pätevä.



c)

1.	$\langle 1\rangle\neg(\Box\Box A \to \Box\Box\Box A)$	
2.	$\langle 1\rangle\Box\Box A$	(1)
3.	$\langle 1\rangle\neg\Box\Box\Box A$	(1)
4.	$\langle 1,2\rangle\neg\Box\Box A$	(3)
5.	$\langle 1,2\rangle\Box A$	(2)
6.	$\langle 1,2,3\rangle\neg\Box A$	(4)
7.	$\langle 1,2,3\rangle A$	(5)
8.	$\langle 1,2,3,4\rangle\neg A$	(6)

Ei **K**-pätevä. $\langle 1\rangle \longrightarrow \langle 1,2\rangle \longrightarrow \overset{A}{\langle 1,2,3\rangle} \longrightarrow \overset{\neg A}{\langle 1,2,3,4\rangle}$