T-79.1001 **Autumn 2005**
Introduction to Theoretical Computer Science T
Tutorial 7, 8–9 November
Problems

Homework problems:

1. Convert the following grammar into Chomsky normal form:

$$\begin{aligned} S &\to AB \mid c \\ A &\to T \mid aA \\ B &\to TT \mid \varepsilon \\ T &\to bS \end{aligned}$$

2. Determine, using the CYK algorithm ("dynamic programming method", Sipser p. 241, Lewis & Papadimitriou p. 155), whether the strings *abba*, *bbaa* and *bbaab* are generated by the grammar

$$\begin{aligned} S &\to AB \mid BA \mid a \mid b \\ A &\to BA \mid a \\ B &\to AB \mid b \end{aligned}$$

   In the positive cases, give also the respective parse trees.

3. Design pushdown automata recognising the following languages:
   (a) $\{w \in \{a,b\}^* \mid w = w^R\}$;
   (b) The language generated by grammar

$$S \to (S) \mid S,S \mid a$$

   (Cf. Tutorial 5, Problem 3.)

Demonstration problems:

4. Design an algorithm for testing whether a given a context-free grammar $G = (V, \Sigma, P, S)$, generates a nonempty language, i.e. whether any terminal string $x \in \Sigma^*$ can be derived from the start symbol S.

5. Design a pushdown automaton corresponding to the grammar $G = (V, \Sigma, P, S)$, where

$$\begin{aligned} V &= \{S, (,), {}^*, \cup, \emptyset, a, b\} \\ \Sigma &= \{(,), {}^*, \cup, \emptyset, a, b\} \\ P &= \{S \to (SS), S \to S^*, S \to (S \cup S), \\ &\quad\; S \to \emptyset, S \to a, S \to b\} \end{aligned}$$

6. Design a grammar corresponding to the pushdown automaton $M = (Q, \Sigma, \Gamma, \Delta, s, F)$, where

$$\begin{aligned} Q =& \{s,q,f\},\ \Sigma = \{a,b\},\ \Gamma = \{a,b,c\},\ F = \{f\}, \\ \Delta =& \big\{\big((s,e,e),(q,c)\big), \big((q,a,c),(q,ac)\big), \big((q,a,a),(q,aa)\big) \\ & \big((q,a,b),(q,e)\big), \big((q,b,c),(q,bc)\big), \big((q,b,b),(q,bb)\big) \\ & \big((q,b,a),(q,e)\big), \big((q,e,c),(f,e)\big)\big\} \end{aligned}$$